



# Cambridge International AS & A Level

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## FURTHER MATHEMATICS

9231/42

Paper 4 Further Probability &amp; Statistics

October/November 2024

1 hour 30 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

### INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

### INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **16** pages. Any blank pages are indicated.





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Find a 90% confidence interval for the population mean length of leaves of this type of plant. [4]

[illegible]



**2** The random variable  $X$  has probability generating function  $G_X(t)$  given by

$$G_X(t) = \frac{1}{5} + pt + qt^2,$$

where  $p$  and  $q$  are constants.

(a) Given that  $E(X) = 1.1$ , find the numerical value of  $\text{Var}(X)$ . [4]

This image shows a full page of a worksheet designed for handwriting practice. It features approximately 20 horizontal rows, each defined by two parallel dotted lines. The lines are evenly spaced and extend across the entire width of the page, providing a guide for letter height and placement. There is no text or other markings on the page.



The random variable  $Y$  has probability generating function  $G_Y(t)$  given by

$$G_Y(t) = \frac{2}{3}t \left( 1 + \frac{1}{2}t^2 \right).$$

The random variable  $Z$  is the sum of independent observations of  $X$  and  $Y$ .

- (b) Find the probability generating function of  $Z$ . [2]

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- (c) Find  $P(Z > 2)$ . [1]

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- (d) State the most probable value of  $Z$ . [1]

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- 4 The random variable  $X$  has probability density function  $f$  given by

$$f(x) = \begin{cases} \frac{1}{21}(x-1)^2 & 2 \leq x \leq 5, \\ 0 & \text{otherwise.} \end{cases}$$

- (a) Find the cumulative distribution function of  $X$ .

[3]

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The random variable  $Y$  is defined by  $Y = (X-1)^4$ .

- (b) Find the probability density function of  $Y$ .

[3]

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(c) Find the median value of  $Y$ .

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(d) Find  $E(Y)$ .

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